

Modelling barred galaxies using analytical potentials

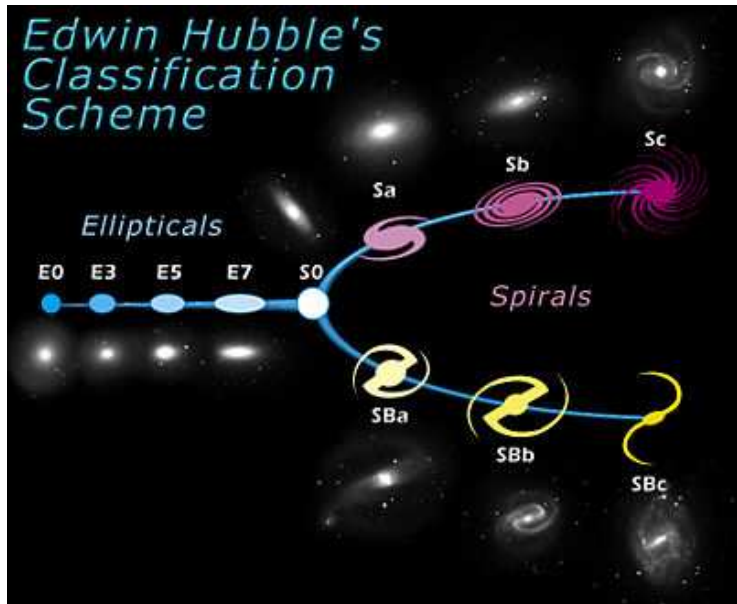
Mercè Romero-Gómez

Working Seminar
UB

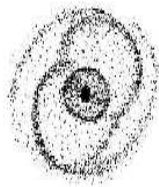
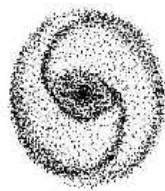
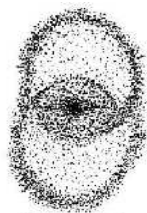
June 12th 2009

collaborators: J.J. Masdemont, E. Athanassoula, T. Antoja, F.
Figueras

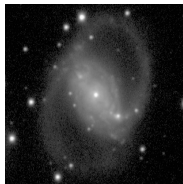
Hubble classification scheme (1925)



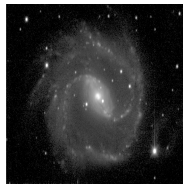
Motivation



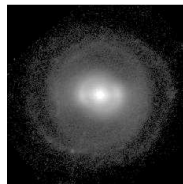
NGC 1365
Spiral arms



NGC 2665
 R_1



NGC 2935
 R_2



NGC 1079
 $R_1 R_2$

Basic characteristics of spiral galaxies - II

- ▶ The rotation curve is typically linearly rising in the central part and flat in the outer region.
- ▶ The sense of winding of the arms with respect to the sense of rotation is mainly trailing.

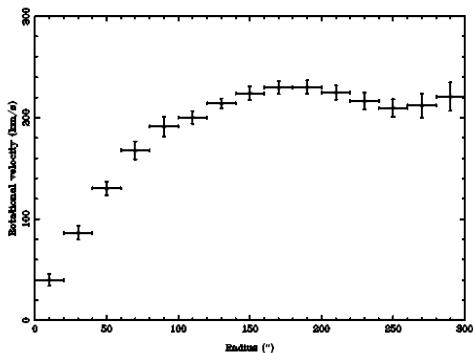


Figure: Rotation curve for NGC 1300; Jörsäter, S. and Moorsel, G.A. (1995)

Why studying barred spiral and ringed galaxies? -I

- ▶ The origin of spiral structure has been one of the main problems in astrophysics and current theories are kind of “slippery”:
 - ▶ Swedish astronomer B. Lindblad proposed that spirals result from the gravitational interaction between the orbits of the stars and the disc.
 - ▶ Therefore, we have to study them from the stellar dynamics point of view.
 - ▶ However, his methods were not appropriate for a quantitative analysis.
 - ▶ Lin and Shu proposed that spirals results from a density wave.
 - ▶ They can use wave mechanics to explain the properties of the density waves.

Why studying barred spiral and ringed galaxies? -II

- ▶ Toomre in the 80s obtains that spirals propagate in the disc from the centre of the galaxy outwards towards one of the principal resonances of the disc, where they damp down:

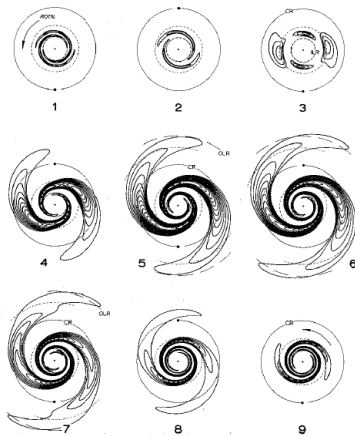


Figure: Toomre (1981)

Obtaining long-lived spirals

Long-lived spirals need replenishment:

- ▶ Swing amplification feed-back cycles.
- ▶ Driven by a companion.
- ▶ Driven by bars.

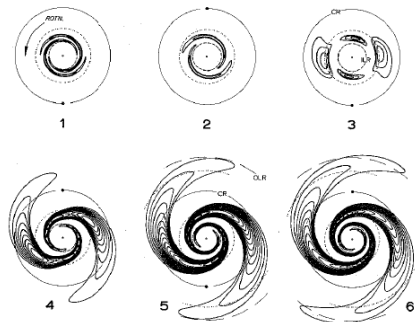
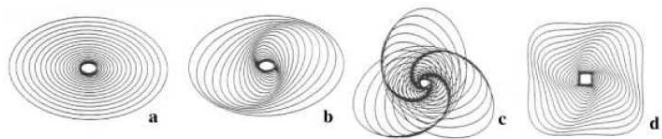
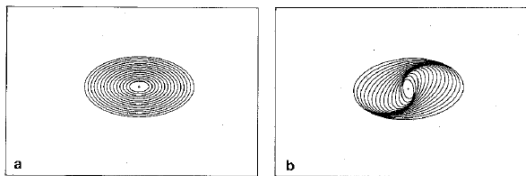


Figure: Toomre (1981)

Kinematic density waves



Rings - N-body simulations

Some theories propose that rings are related to the principal resonances of the galaxy:

- ▶ ILR related to Nuclear rings
- ▶ CR related to Inner rings
- ▶ OLR related to Outer rings

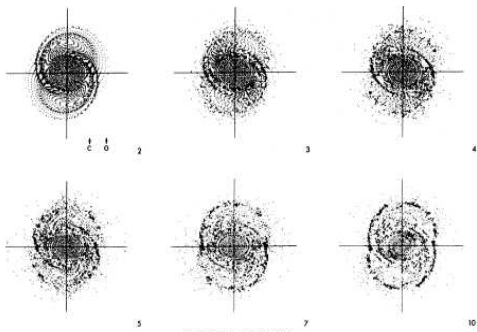
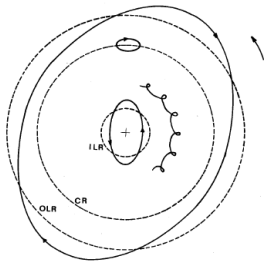
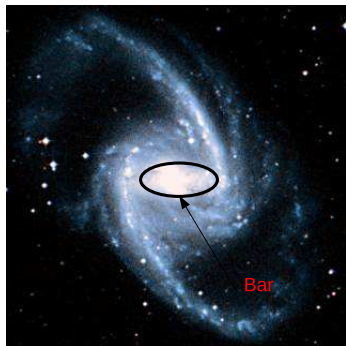


Figure: Schwarz, M.P. (1981)

Components of a barred galaxy



Bar models consist of the superposition of

- ▶ Axisymmetric component:
 - ▶ a disc: Miyamoto-Nagai, Kuzmin/Toomre potentials.
 - ▶ a spheroid or bulge: Plummer, spherical potentials.
 - ▶ a Halo: spherical potential.
- ▶ a bar: Ferrers ellipsoids, ad-hoc bar potentials, logarithmic, analytical potentials that match observations.
- ▶ (spiral arms: logarithmic, superposition of ellipsoids.)

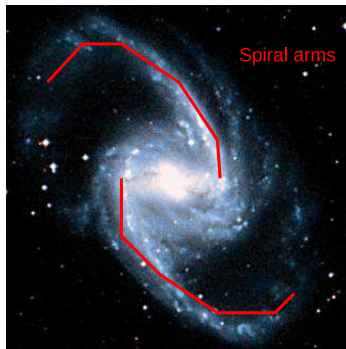
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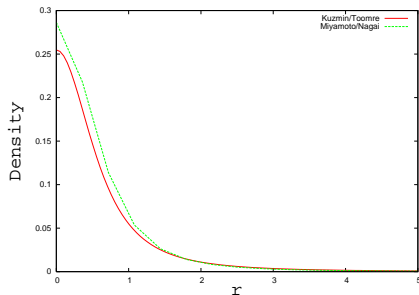
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The disc

- ▶ Discs are flattened, roughly axisymmetric, disc-like structures.
- ▶ They have an exponential surface-brightness distribution.
- ▶ Represented by Miyamoto-Nagai or Kuzmin/Toomre disc potentials.

$$\Phi_M(R) = -\frac{GM}{\sqrt{R^2 + A^2}}$$

$$\Phi_K(R) = -\frac{3}{2}V_0^2 \left(\frac{3/2}{1/2 + R^2/r_0^2} \right)^{1/2}$$



The spheroid/halo

- ▶ They are roughly spherical distributions of stars.
- ▶ Represented by a Plummer spheroid or any spheric density distribution.

$$\rho_P(R) = \left(\frac{3M}{4\pi B^3} \right) \left(1 + \frac{R^2}{B^2} \right)^{-5/2}$$

$$\rho(R) = \rho_b \left(1 + \frac{R^2}{r_b^2} \right)^{-3/2}$$

The density and the potential are related via the Poisson's equation: $\nabla^2\Phi = 4\pi G\rho$.

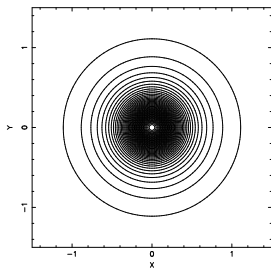
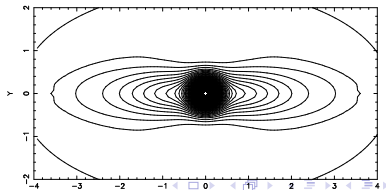
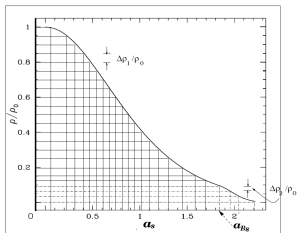
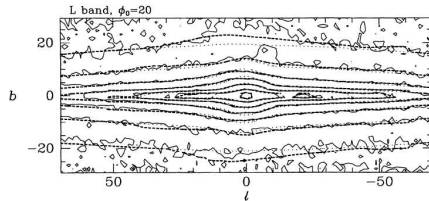


Figure: Isodensity curves for the spheroid.

Bar characteristics

- ▶ Bars are non-axisymmetric triaxial features with high ellipticities. The typical axes have length scales proportional to 1:2.
- ▶ Bars are not centrally condensed. The surface brightness is
 - ▶ nearly constant along the semi-major axis.
 - ▶ steep and falls off sharply along the semi-minor axis.
- ▶ Bars extend up to CR. The ratio $R_{CR}/a = 1.2 \pm 0.2$ and rotate fast.

Bar component - From observations to the potential



Bar component - Density functions

► Ferrer's ellipsoid: $\rho = \begin{cases} \rho_0(1 - m^2)^n & m \leq 1 \\ 0 & m \geq 1, \end{cases}$

$$m^2 = x^2/a^2 + y^2/b^2 + z^2/c^2.$$

- Superposition of homogeneous ellipsoids

$$\rho = \begin{cases} \rho_0 \operatorname{sech}^2(R_s) & 0 \leq R_s \leq R_{end} \\ \rho_0 \operatorname{sech}^2(R_s) e^{-(R_s - R_{end})/h^2} & R_s \geq R_{end} \end{cases}$$

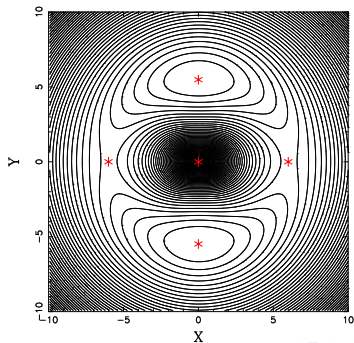
Ad-hoc bar potentials

These are potentials of “m=2”-type: $\phi(r, \theta) = A(r) \cos(2\theta)$.

- ▶ Dehnen's bar type:

$$\Phi(r, \theta) = -\frac{1}{2}\epsilon v_0^2 \cos(2\theta) \begin{cases} 2 - \left(\frac{r}{a}\right)^n, & r \leq a \\ \left(\frac{a}{r}\right)^n, & r \geq a \end{cases}$$

- ▶ Barbanis-Woltjer's type: $\Phi(r, \theta) = \hat{\epsilon}\sqrt{r}(r_1 - r) \cos(2\theta)$

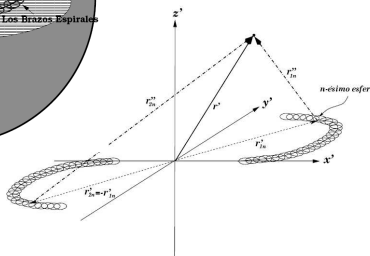
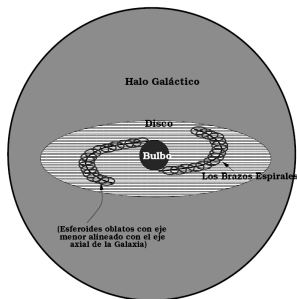


Spiral component

- ▶ Superposition of ellipsoids of locus:

$$\phi(R) = -\left(\frac{m}{N \tan i}\right) \ln [1 + (R/R_s)^N]$$

Each spheroid: i) potential given by the analytical, ii) lineal density law, iii) exponential decay of the central density of each spheroid.



Combination of bar+spiral component

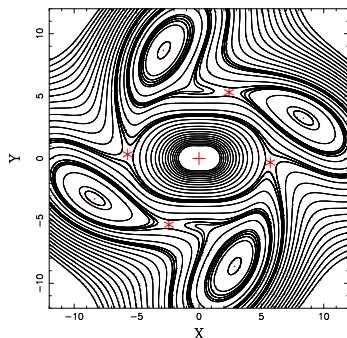
- ▶ Bar+spiral: density:

$$S(r, \theta) = A(r) \begin{cases} \cos(2\theta) & , r \leq a \\ \cos(2\theta - \phi(r)) & , r \geq a \end{cases}$$

More than two arms?

We can obtain 4-armed spirals with a potential of the type:

$$\Phi(r, \theta) = A_2(r) \cos(2\theta) + A_4(r) \cos(4\theta + \phi(r) + \theta_0).$$



Equations of motion

- ▶ The potential: $\Phi = \Phi_s + \Phi_d + \Phi_b$
- ▶ The equations of motion of a rotating system are described in vectorial form by:

$$\ddot{\mathbf{r}} = -\nabla\Phi_{\text{eff}} - 2(\boldsymbol{\Omega} \times \dot{\mathbf{r}}),$$

where $\mathbf{r} = (x, y, z)$ is the position vector and $\boldsymbol{\Omega} = (0, 0, \Omega)$ is the rotation velocity vector around the z-axis, and $\Phi_{\text{eff}} = \Phi - \frac{1}{2}\Omega^2(x^2 + y^2)$ is the effective potential.

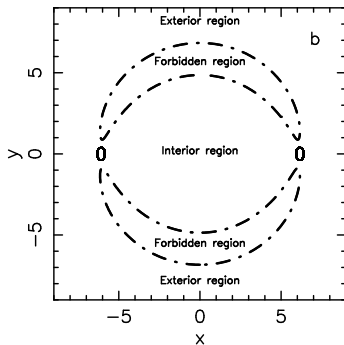
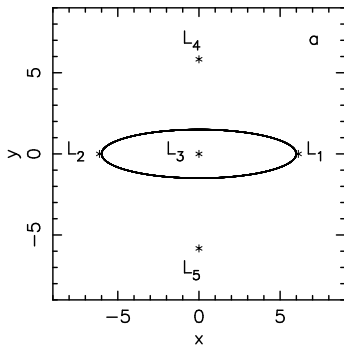
- ▶ We define the Jacobi constant or Jacobi energy as $E_J = \frac{1}{2}|\dot{\mathbf{r}}|^2 + \Phi_{\text{eff}}$.
- ▶ The zero velocity surface of a given energy level is the surface obtained when: $\Phi_{\text{eff}}(x, y, z) = E_J$. We define the zero velocity curve, its cut with the $z = 0$ plane.

Equilibrium points

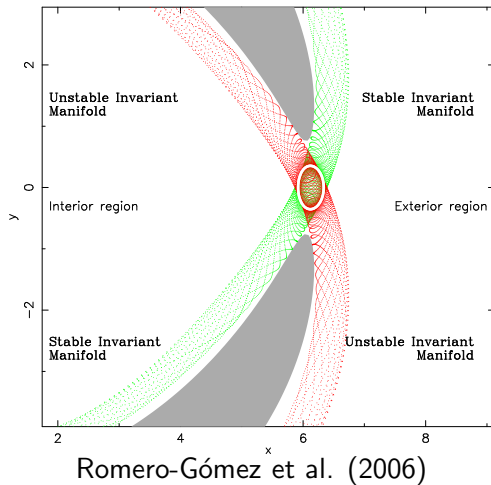
- ▶ The equilibrium points of the system are located where

$$\frac{\partial \Phi_{\text{eff}}}{\partial x} = \frac{\partial \Phi_{\text{eff}}}{\partial y} = \frac{\partial \Phi_{\text{eff}}}{\partial z} = 0.$$

They lie on the xy -plane: L_1 and L_2 along the bar major axis, L_3 on the origin, and L_4 and L_5 along the bar minor axis.



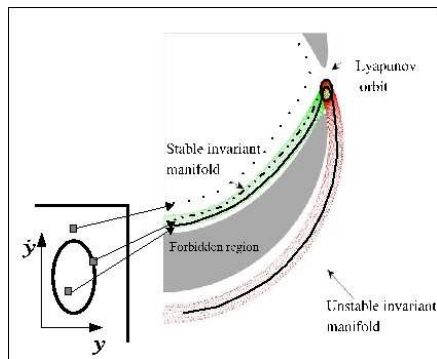
Nonlinear stable and unstable invariant manifolds



Transit orbits

Transfer of matter from the interior to the exterior region:

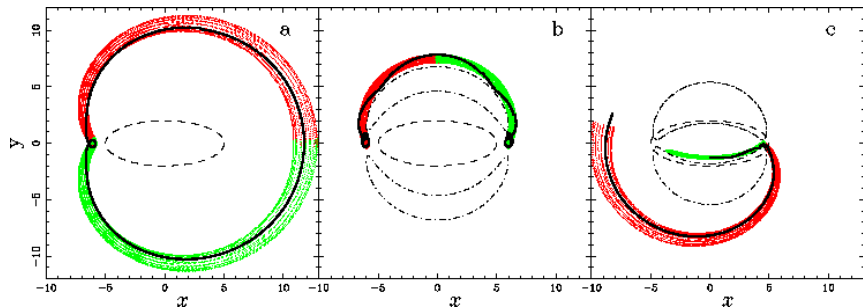
- ▶ Transit orbits have initial conditions *inside* the $W_{\gamma_i}^{s,1}$ curve in the $y\dot{y}$ plane.
- ▶ Non-transit orbits have initial conditions *outside* the $W_{\gamma_i}^{s,1}$ curve in the $y\dot{y}$ plane.



Transfer of matter: Homoclinic and heteroclinic orbits

- ▶ Homoclinic orbits, ψ , s.t. $\psi \in W_{\gamma_i}^u \cap W_{\gamma_i}^s$, $i = 1, 2$
- ▶ Heteroclinic orbits, ψ' , s.t. $\psi' \in W_{\gamma_i}^u \cap W_{\gamma_j}^s$, $i \neq j$, $i, j = 1, 2$

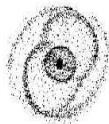
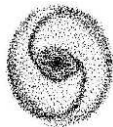
Romero-Gómez et al. (2007)



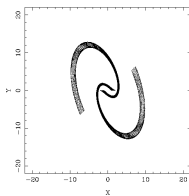
Homoclinic

Heteroclinic

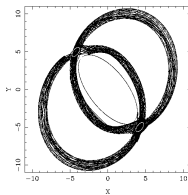
Transit



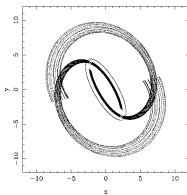
d - Barred spiral structure - projected



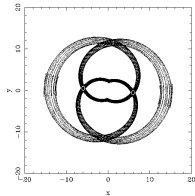
a - rR1 ring structure - projected



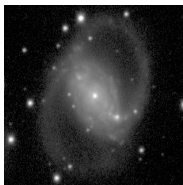
b - rR2 ring structure - projected



e - rR1R2 ring structure - projected



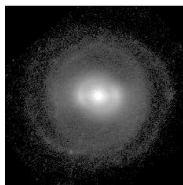
NGC 1365
Spiral arms



NGC 2665
 R_1



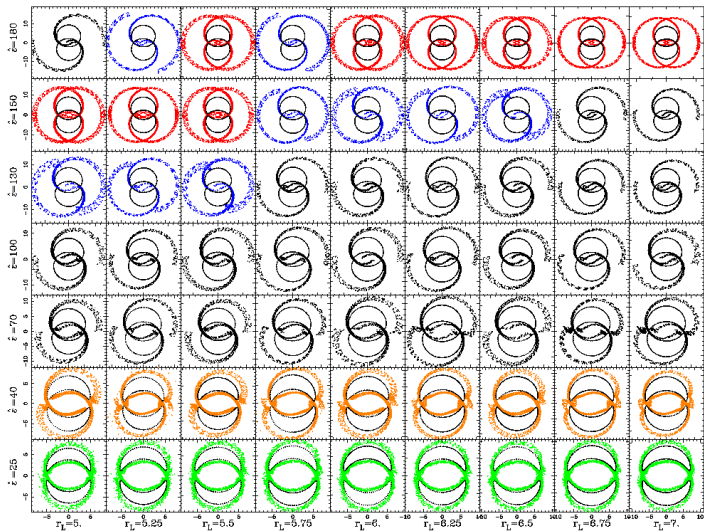
NGC 2935
 R_2



NGC 1079
 $R_1 R_2$

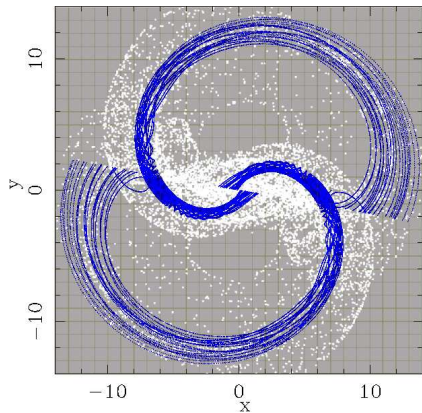
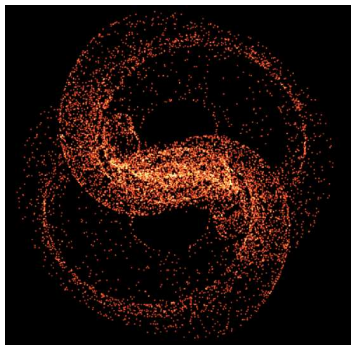
2D parameter study - BW type of bar

Athanassoula, Romero-Gómez & Masdemont (2009)



Simulation - response. Where does all the material on these orbits comes from? Only from the immediate neighbourhood of the Lagrangian points?

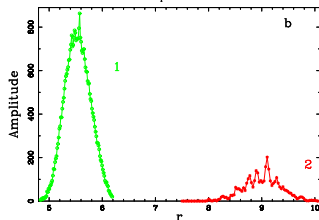
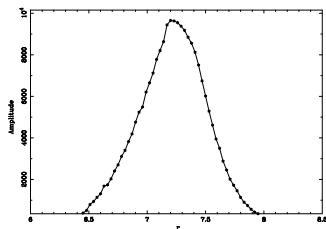
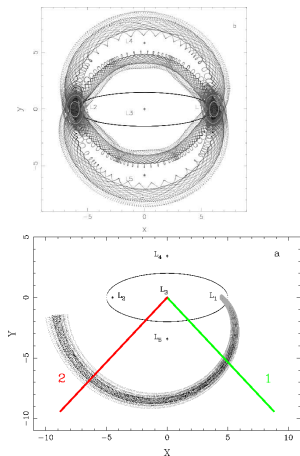
Not necessarily. In fact, most of it can come from the outer parts of the bar, driven to the L_1/L_2 and to the unstable manifold by the inner branch of the stable manifold.



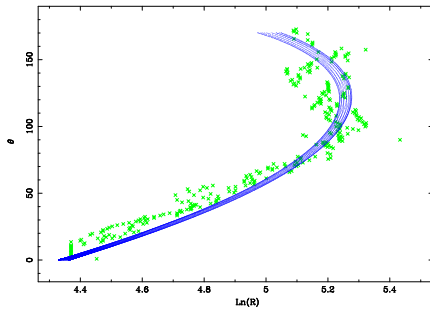
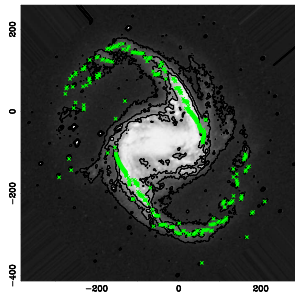
Photometrics: Radial profile

The density profile along a cut across the ring and spiral arms has the same properties as in observations.

Romero-Gómez et al. (2006)



Photometrics: Pitch angle



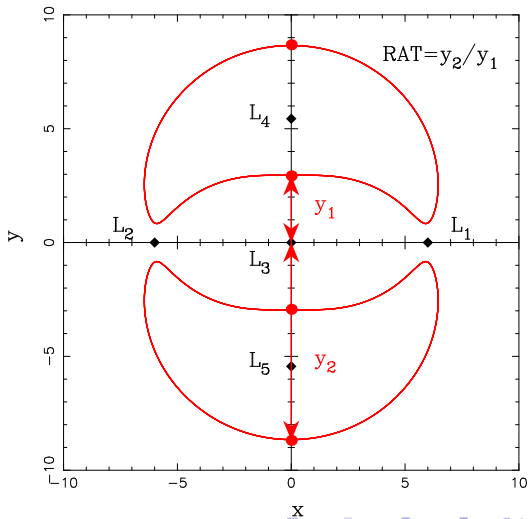
Is there a quantity, valid for all barred galaxy potentials, that can predict whether a model/galaxy will be spiral, R_1 , R_2 or R_1R_2 ? Yes (?)

▶ $q_r = \frac{\partial\Phi_2/\partial r}{\partial\Phi_0/\partial r}$

▶ $q_t = \frac{(\partial\Phi/\partial\theta)_{max}}{r\partial\Phi_0/\partial r}$

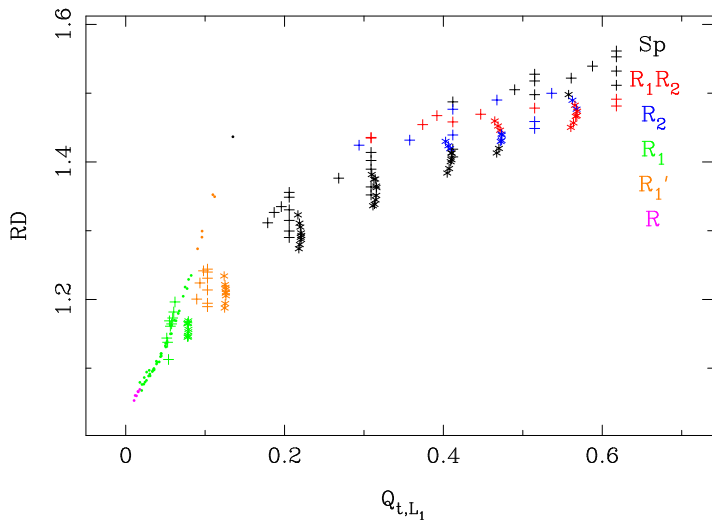
▶ $\Phi_{eff} = \Phi - \frac{1}{2}\Omega_p^2(x^2 + y^2)$

▶ $RAT = \frac{y_2}{y_1}$



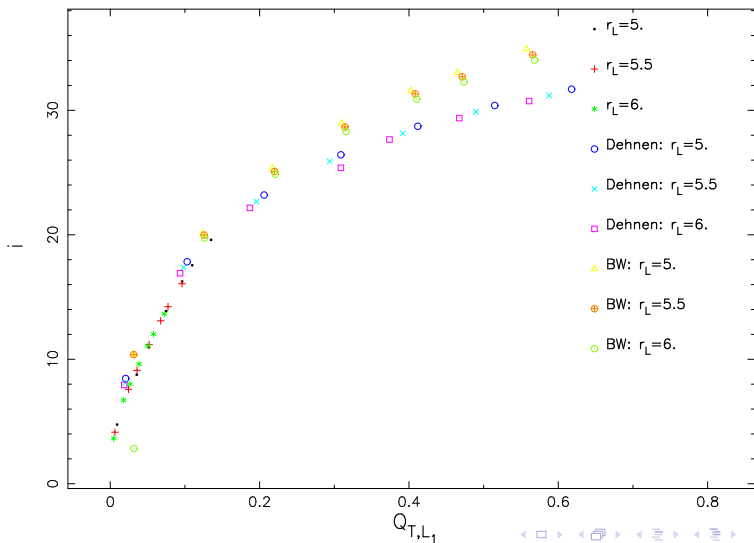
2D parameter study - prediction tool

Athanassoula, Romero-Gómez & Masdemont (2009)



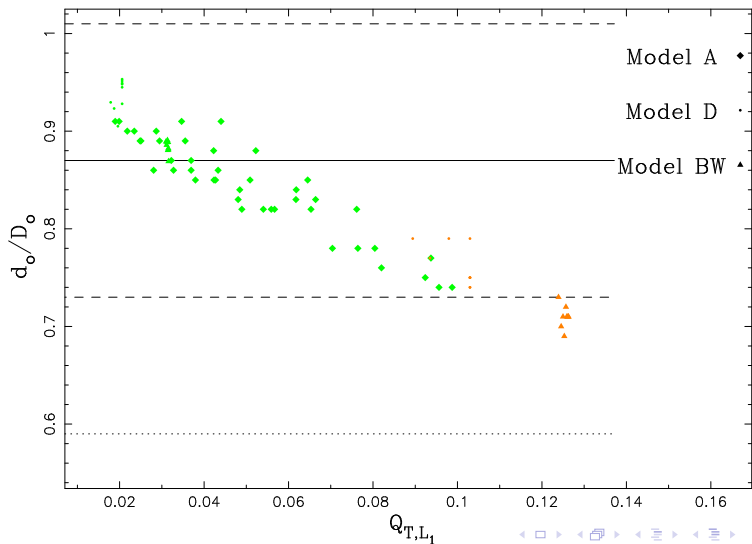
Pitch angle vs strength parameter

According to observations, the pitch angle of the spiral arm increases in galaxies with a strong bar.



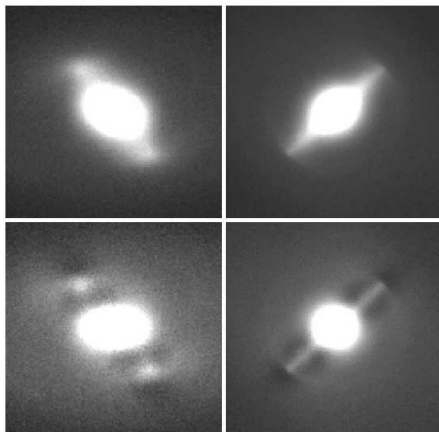
Ratio of the outer ring diameters vs strength parameter

We find a good correlation between the ratio of the outer ring diameters with the strength of the bar.



Stabilisation of L_1 and L_2 - ansae formation? -I

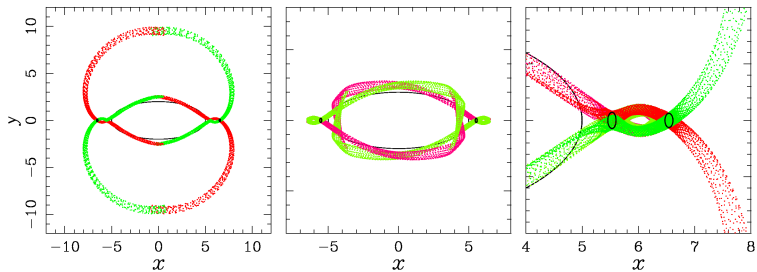
What if material gets concentrated at the ends of the bar?



ansae bars

"normal" bars

Stabilisation of L_1 and L_2 - ansae formation? -II



Summary

- ▶ Here we propose a new theory on the formation of spiral arms and rings in barred galaxy, from the dynamical systems point of view.
- ▶ We studied the dynamics of the L_1 and L_2 unstable Lagrangian points, of the Lyapounov orbits and of the invariant manifolds.
- ▶ The manifolds:
 - ▶ They extend far from the unstable Lagrangian points L_1 and L_2 and thus can drive global structures
 - ▶ They have the right shapes and reproduce all known types of spiral and ring shapes (R_1 , R_2 , R_1R_2)
 - ▶ Their photometric radial profiles are in global agreement with observations (Schweizer 1976)
 - ▶ The loci they outline agrees well with the high density regions in simulations
- ▶ The unstable and stable invariant manifolds could be the building blocks for spiral and rings in barred galaxies.

The Milky Way

